Introduction to Information Retrieval
http://informationretrieval.org

IIR 4: Index Construction

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Overview

1. Recap
2. Introduction
3. BSBI algorithm
4. SPIMI algorithm
5. Distributed indexing
6. Dynamic indexing
Outline

1. Recap
2. Introduction
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6. Dynamic indexing
Dictionary as array of fixed-width entries

<table>
<thead>
<tr>
<th>term</th>
<th>document frequency</th>
<th>pointer to postings list</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>656,265</td>
<td>→</td>
</tr>
<tr>
<td>aachen</td>
<td>65</td>
<td>→</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>zulu</td>
<td>221</td>
<td>→</td>
</tr>
</tbody>
</table>

space needed: 20 bytes 4 bytes 4 bytes
### Recap

<table>
<thead>
<tr>
<th>Introduction</th>
<th>BSBI algorithm</th>
<th>SPIMI algorithm</th>
<th>Distributed indexing</th>
<th>Dynamic indexing</th>
</tr>
</thead>
</table>

#### B-tree for looking up entries in array

![B-tree Diagram]

**ISR: Index construction**
Wildcard queries using a permuterm index

Queries:
- For $X$, look up $X$
- For $X^*$, look up $X^*$
- For $^*X$, look up $X^*$
- For $^*X^*$, look up $X^*$
- For $X^*Y$, look up $Y^*X^*$
$k$-gram indexes for spelling correction: bordroom
Levenshtein distance for spelling correction

\[
\text{LEVENSHTEIN}\text{DISTANCE}(s_1, s_2)
\]
\[
\begin{align*}
1 & \text{ for } i \leftarrow 0 \text{ to } |s_1| \\
2 & \text{ do } m[i, 0] = i \\
3 & \text{ for } j \leftarrow 0 \text{ to } |s_2| \\
4 & \text{ do } m[0, j] = j \\
5 & \text{ for } i \leftarrow 1 \text{ to } |s_1| \\
6 & \text{ do for } j \leftarrow 1 \text{ to } |s_2| \\
7 & \quad \text{ if } s_1[i] = s_2[j] \\
8 & \quad \quad \text{ then } m[i, j] = \min\{m[i-1, j] + 1, m[i, j-1] + 1, m[i-1, j-1]\} \\
9 & \quad \quad \text{ else } m[i, j] = \min\{m[i-1, j] + 1, m[i, j-1] + 1, m[i-1, j-1] + 1\} \\
10 & \quad \text{ return } m[|s_1|, |s_2|]
\end{align*}
\]

Operations: insert, delete, replace, copy
Take-away

- Two index construction algorithms: BSBI (simple) and SPIMI (more realistic)
- **Distributed** index construction: MapReduce
- **Dynamic** index construction: how to keep the index up-to-date as the collection changes
Many design decisions in information retrieval are based on hardware constraints.

We begin by reviewing hardware basics that we’ll need in this course.
Access to data is much faster in memory than on disk. (roughly a factor of 10)

Disk seeks are “idle” time: No data is transferred from disk while the disk head is being positioned.

To optimize transfer time from disk to memory: one large chunk is faster than many small chunks.

Disk I/O is block-based: Reading and writing of entire blocks (as opposed to smaller chunks). Block sizes: 8KB to 256 KB.

Servers used in IR systems typically have many GBs of main memory and TBs of disk space.

Fault tolerance is expensive: It’s cheaper to use many regular machines than one fault tolerant machine.
### Some stats (ca. 2008)

<table>
<thead>
<tr>
<th>symbol</th>
<th>statistic</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(s)</td>
<td>average seek time</td>
<td>(5 \text{ ms} = 5 \times 10^{-3} \text{ s})</td>
</tr>
<tr>
<td>(b)</td>
<td>transfer time per byte</td>
<td>(0.02 , \mu\text{s} = 2 \times 10^{-8} \text{ s})</td>
</tr>
<tr>
<td></td>
<td>processor’s clock rate</td>
<td>(10^9 \text{ s}^{-1})</td>
</tr>
<tr>
<td>(p)</td>
<td>lowlevel operation (e.g., compare &amp; swap a word)</td>
<td>(0.01 , \mu\text{s} = 10^{-8} \text{ s})</td>
</tr>
<tr>
<td></td>
<td>size of main memory</td>
<td>several GB</td>
</tr>
<tr>
<td></td>
<td>size of disk space</td>
<td>1 \text{ TB or more}</td>
</tr>
</tbody>
</table>
Shakespeare’s collected works are not large enough for demonstrating many of the points in this course.

As an example for applying scalable index construction algorithms, we will use the Reuters RCV1 collection.

English newswire articles sent over the wire in 1995 and 1996 (one year).
Extreme conditions create rare Antarctic clouds

SYDNEY (Reuters) - Rare, mother-of-pearl colored clouds caused by extreme weather conditions above Antarctica are a possible indication of global warming, Australian scientists said on Tuesday.

Known as nacreous clouds, the spectacular formations showing delicate wisps of color were photographed in the sky over an Australian
## Reuters RCV1 statistics

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N$</td>
<td>documents</td>
<td>800,000</td>
</tr>
<tr>
<td>$L$</td>
<td>tokens per document</td>
<td>200</td>
</tr>
<tr>
<td>$M$</td>
<td>terms (= word types)</td>
<td>400,000</td>
</tr>
<tr>
<td></td>
<td>bytes per token (incl. spaces/punct.)</td>
<td>6</td>
</tr>
<tr>
<td></td>
<td>bytes per token (without spaces/punct.)</td>
<td>4.5</td>
</tr>
<tr>
<td></td>
<td>bytes per term (= word type)</td>
<td>7.5</td>
</tr>
<tr>
<td>$T$</td>
<td>non-positional postings</td>
<td>100,000,000</td>
</tr>
</tbody>
</table>
Outline

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Goal: construct the inverted index

<table>
<thead>
<tr>
<th>Name</th>
<th>Postings</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brutus</td>
<td>1 2 4 11 31 45 173 174</td>
</tr>
<tr>
<td>Caesar</td>
<td>1 2 4 5 6 16 57 132 ...</td>
</tr>
<tr>
<td>Calpurnia</td>
<td>2 31 54 101</td>
</tr>
</tbody>
</table>

...
Index construction in IIR 1: Sort postings in memory

<table>
<thead>
<tr>
<th>term</th>
<th>docID</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>1</td>
</tr>
<tr>
<td>did</td>
<td>1</td>
</tr>
<tr>
<td>enact</td>
<td>1</td>
</tr>
<tr>
<td>julius</td>
<td>1</td>
</tr>
<tr>
<td>caesar</td>
<td>1</td>
</tr>
<tr>
<td>I</td>
<td>1</td>
</tr>
<tr>
<td>was</td>
<td>1</td>
</tr>
<tr>
<td>killed</td>
<td>1</td>
</tr>
<tr>
<td>i'</td>
<td>1</td>
</tr>
<tr>
<td>the</td>
<td>1</td>
</tr>
<tr>
<td>capitol</td>
<td>1</td>
</tr>
<tr>
<td>brutus</td>
<td>1</td>
</tr>
<tr>
<td>killed</td>
<td>1</td>
</tr>
<tr>
<td>me</td>
<td>1</td>
</tr>
<tr>
<td>so</td>
<td>2</td>
</tr>
<tr>
<td>let</td>
<td>2</td>
</tr>
<tr>
<td>it</td>
<td>2</td>
</tr>
<tr>
<td>be</td>
<td>2</td>
</tr>
<tr>
<td>with</td>
<td>2</td>
</tr>
<tr>
<td>caesar</td>
<td>2</td>
</tr>
<tr>
<td>the</td>
<td>2</td>
</tr>
<tr>
<td>noble</td>
<td>2</td>
</tr>
<tr>
<td>brutus</td>
<td>2</td>
</tr>
<tr>
<td>hath</td>
<td>2</td>
</tr>
<tr>
<td>told</td>
<td>2</td>
</tr>
<tr>
<td>you</td>
<td>2</td>
</tr>
<tr>
<td>caesar</td>
<td>2</td>
</tr>
<tr>
<td>was</td>
<td>2</td>
</tr>
<tr>
<td>ambitious</td>
<td>2</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>term</th>
<th>docID</th>
</tr>
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<tbody>
<tr>
<td>ambitious</td>
<td>2</td>
</tr>
<tr>
<td>be</td>
<td>2</td>
</tr>
<tr>
<td>brutus</td>
<td>1</td>
</tr>
<tr>
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<td>2</td>
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<tr>
<td>capitol</td>
<td>1</td>
</tr>
<tr>
<td>caesar</td>
<td>1</td>
</tr>
<tr>
<td>caesar</td>
<td>2</td>
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<tr>
<td>did</td>
<td>1</td>
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<td>1</td>
</tr>
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<td>1</td>
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<tr>
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<td>1</td>
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<tr>
<td>i'</td>
<td>1</td>
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<td>1</td>
</tr>
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<td>brutus</td>
<td>1</td>
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<tr>
<td>killed</td>
<td>1</td>
</tr>
<tr>
<td>me</td>
<td>1</td>
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<tr>
<td>so</td>
<td>2</td>
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<tr>
<td>let</td>
<td>2</td>
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<td>it</td>
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</tr>
<tr>
<td>the</td>
<td>2</td>
</tr>
<tr>
<td>told</td>
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<td>2</td>
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<tr>
<td>was</td>
<td>2</td>
</tr>
<tr>
<td>was</td>
<td>2</td>
</tr>
<tr>
<td>with</td>
<td>2</td>
</tr>
</tbody>
</table>
Sort-based index construction

- As we build index, we parse docs one at a time.
- The final postings for any term are incomplete until the end.
- Can we keep all postings in memory and then do the sort in-memory at the end?
- No, not for large collections
- Thus: We need to store intermediate results on disk.
Same algorithm for disk?

- Can we use the same index construction algorithm for larger collections, but by using disk instead of memory?
- No: Sorting very large sets of records on disk is too slow – too many disk seeks.
- We need an external sorting algorithm.
We must sort $T = 100,000,000$ non-positional postings.
- Each posting has size 12 bytes (4+4+4: termID, docID, term frequency).

Define a **block** to consist of 10,000,000 such postings
- We can easily fit that many postings into memory.
- We will have 10 such blocks for RCV1.

**Basic idea of algorithm:**
- For each block: (i) accumulate postings, (ii) sort in memory, (iii) write to disk
- Then merge the blocks into one long sorted order.
Merging two blocks

postings
to be merged

Block 1
brutus   d3
caesar   d4
noble    d3
with     d4

Block 2
brutus   d2
caesar   d1
julius   d1
killed   d2

merged postings

brutus d2
brutus d3
caesar d1
caesar d4
julius d1
killed d2
noble d3
with d4

disk
Blocked Sort-Based Indexing

**BSBI**\_\_**IndexConstruction**() 

1. $n \leftarrow 0$
2. while (all documents have not been processed) 
3. \hspace{1em} do $n \leftarrow n + 1$
4. \hspace{2em} block $\leftarrow$ **ParseNextBlock**() 
5. \hspace{2em} **BSBI-\text{Invert}(block)** 
6. \hspace{2em} **WriteBlockToDisk**(block, $f_n$) 
7. \hspace{2em} **MergeBlocks**($f_1, \ldots, f_n; f_{\text{merged}}$)
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Problem with sort-based algorithm

- Our assumption was: we can keep the dictionary in memory.
- We need the dictionary (which grows dynamically) in order to implement a term to termID mapping.
- Actually, we could work with term,docID postings instead of termID,docID postings . . .
- . . . but then intermediate files become very large. (We would end up with a scalable, but very slow index construction method.)
Abbreviation: SPIMI

Key idea 1: Generate separate dictionaries for each block – no need to maintain term-termID mapping across blocks.

Key idea 2: Don’t sort. Accumulate postings in postings lists as they occur.

With these two ideas we can generate a complete inverted index for each block.

These separate indexes can then be merged into one big index.
SPIMI-Invert

SPIMI-Invert\((token\_stream)\)
1 \(output\_file \leftarrow \text{NEWFILE}()\)
2 \(dictionary \leftarrow \text{NEWHASH}()\)
3 \(\textbf{while} \ (\text{free memory available})\)
4 \(\textbf{do} \ \text{token} \leftarrow \text{next}(token\_stream)\)
5 \(\textbf{if} \ \text{term(token)} \notin \text{dictionary}\)
6 \(\textbf{then} \ \text{postings}\_\text{list} \leftarrow \text{ADDTODIRECTORY}(dictionary, \text{term(token)})\)
7 \(\text{else} \ \text{postings}\_\text{list} \leftarrow \text{GETPOSTINGSLIST}(dictionary, \text{term(token)})\)
8 \(\textbf{if} \ \text{full}(\text{postings}\_\text{list})\)
9 \(\textbf{then} \ \text{postings}\_\text{list} \leftarrow \text{DOUBLEPOSTINGSLIST}(dictionary, \text{term(token)})\)
10 \(\text{ADDTOPOSTINGSLIST}(postings\_list, \text{docID(token)})\)
11 \(\text{sorted}\_\text{terms} \leftarrow \text{SORTTERMS}(dictionary)\)
12 \(\text{WRITEBLOCKTODISK}(sorted\_\text{terms}, dictionary, output\_file)\)
13 \(\textbf{return} \ output\_file\)

Merging of blocks is analogous to BSBI.
Compression makes SPIMI even more efficient.

- Compression of terms
- Compression of postings
- See next lecture
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Distributed indexing

- For web-scale indexing (don’t try this at home!): must use a distributed computer cluster
- Individual machines are fault-prone.
  - Can unpredictably slow down or fail.
- How do we exploit such a pool of machines?
Google data centers (2007 estimates; Gartner)

- Google data centers mainly contain commodity machines.
- Data centers are distributed all over the world.
- 1 million servers, 3 million processors/cores
- Google installs 100,000 servers each quarter.
- Based on expenditures of 200–250 million dollars per year
- This would be 10% of the computing capacity of the world!
- If in a non-fault-tolerant system with 1000 nodes, each node has 99.9% uptime, what is the uptime of the system (assuming it does not tolerate failures)?
  - Answer: 37%
- Suppose a server will fail after 3 years. For an installation of 1 million servers, what is the interval between machine failures?
  - Answer: less than two minutes
Distributed indexing

- Maintain a master machine directing the indexing job – considered “safe”
- Break up indexing into sets of parallel tasks
- Master machine assigns each task to an idle machine from a pool.
Parallel tasks

- We will define two sets of parallel tasks and deploy two types of machines to solve them:
  - Parsers
  - Inverters
- Break the input document collection into \textit{splits} (corresponding to blocks in BSBI/SPIMI)
- Each split is a subset of documents.
Parsers

- Master assigns a split to an idle parser machine.
- Parser reads a document at a time and emits (term, docID)-pairs.
- Parser writes pairs into $j$ term-partitions.
- Each for a range of terms’ first letters
  - E.g., a-f, g-p, q-z (here: $j = 3$)
Inverters

- An inverter collects all (term, docID) pairs (= postings) for one term-partition (e.g., for a-f).
- Sorts and writes to postings lists
Data flow

splits → assign → master → assign → postings

map phase

segment files

reduce phase

parser

parser

parser

parser

inverter

inverter

inverter

inverter

a-f, g-p, q-z

a-f, g-p, q-z

a-f, g-p, q-z

a-f, g-p, q-z

a-f

g-p

q-z
The index construction algorithm we just described is an instance of MapReduce.

MapReduce is a robust and conceptually simple framework for distributed computing . . .

. . . without having to write code for the distribution part.

The Google indexing system (ca. 2002) consisted of a number of phases, each implemented in MapReduce.

Index construction was just one phase.

Another phase: transform term-partitioned into document-partitioned index.
Index construction in MapReduce

**Schema of map and reduce functions**

- map: input → list\((k, v)\)
- reduce: \((k, \text{list}(v))\) → output

**Instantiation of the schema for index construction**

- map: web collection → list(\(\text{termID}, \text{docID}\))
- reduce: \((\langle \text{termID}_1, \text{list(\text{docID})} \rangle, \langle \text{termID}_2, \text{list(\text{docID})} \rangle, \ldots)\) → \((\text{postings}_{\text{list}_1}, \text{postings}_{\text{list}_2}, \ldots)\)

**Example for index construction**

map: \(d_2: \text{C DIED.} \quad d_1: \text{C CAME, C c’ED.}\) → \((\langle \text{C, } d_2 \rangle, \langle \text{DIED, } d_2 \rangle, \langle \text{C, } d_1 \rangle, \langle \text{CAME, } d_1 \rangle, \langle \text{C, } d_1 \rangle, \langle \text{c’ED, } d_1 \rangle)\)

reduce: \((\langle \text{C, } d_2, d_1 \rangle), \langle \text{DIED, } d_2 \rangle, \langle \text{CAME, } d_1 \rangle, \langle \text{c’ED, } d_1 \rangle)\) → \((\langle \text{C, } d_1:2, d_2:1 \rangle), \langle \text{DIED, } d_2:1 \rangle, \langle \text{CAME, } d_1:1 \rangle, \langle \text{c’ED, } d_1:1 \rangle)\)
Exercise

- What information does the task description contain that the master gives to a parser?
- What information does the parser report back to the master upon completion of the task?
- What information does the task description contain that the master gives to an inverter?
- What information does the inverter report back to the master upon completion of the task?
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Dynamic indexing

- Up to now, we have assumed that collections are \textit{static}.  
- They rarely are: Documents are inserted, deleted and modified.
- This means that the dictionary and postings lists have to be \textit{dynamically} modified.
Dynamic indexing: Simplest approach

- Maintain **big main index on disk**
- New docs go into **small auxiliary index in memory**.
- Search across both, merge results
- Periodically, merge auxiliary index into big index
- Deletions:
  - Invalidation bit-vector for deleted docs
  - Filter docs returned by index using this bit-vector
Issue with auxiliary and main index

- Frequent merges
- Poor search performance during index merge
Logarithmic merge

- Logarithmic merging amortizes the cost of merging indexes over time.
  - → Users see smaller effect on response times.
- Maintain a series of indexes, each twice as large as the previous one.
- Keep smallest ($Z_0$) in memory
- Larger ones ($I_0, I_1, \ldots$) on disk
- If $Z_0$ gets too big ($> n$), write to disk as $I_0$
- \ldots or merge with $I_0$ (if $I_0$ already exists) and write merger to $I_1$ etc.
**LMergeAddToken** *(indexes, Z₀, token)*

1. \( Z₀ \leftarrow \text{Merge}(Z₀, \{ \text{token} \}) \)
2. \( \text{if } |Z₀| = n \)
3. \( \text{then for } i \leftarrow 0 \text{ to } \infty \)
4. \( \text{do if } lᵢ \in \text{indexes} \)
5. \( \text{then } Zᵢ₊₁ \leftarrow \text{Merge}(lᵢ, Zᵢ) \)
6. \( (Zᵢ₊₁ \text{ is a temporary index on disk.}) \)
7. \( \text{indexes } \leftarrow \text{indexes } - \{ lᵢ \} \)
8. \( \text{else } lᵢ \leftarrow Zᵢ \text{ (Zᵢ becomes the permanent index } lᵢ. ) \)
9. \( \text{indexes } \leftarrow \text{indexes } \cup \{ lᵢ \} \)
10. \( \text{Break} \)
11. \( Z₀ \leftarrow \emptyset \)

**LogarithmicMerge()**

1. \( Z₀ \leftarrow \emptyset \text{ (Z₀ is the in-memory index.)} \)
2. \( \text{indexes } \leftarrow \emptyset \)
3. \( \text{while true} \)
4. \( \text{do LMergeAddToken(indexes, Z₀, getNextToken())} \)
Binary numbers: $l_3l_2l_1l_0 = 2^32^22^12^0$

- 0001
- 0010
- 0011
- 0100
- 0101
- 0110
- 0111
- 1000
- 1001
- 1010
- 1011
- 1100
Logarithmic merge

- Number of indexes bounded by $O(\log T)$ ($T$ is total number of postings read so far)
- So query processing requires the merging of $O(\log T)$ indexes
- Time complexity of index construction is $O(T \log T)$.
  - ...because each of $T$ postings is merged $O(\log T)$ times.
- Auxiliary index: index construction time is $O(T^2)$ as each posting is touched in each merge.
  - Suppose auxiliary index has size $a$
  - $a + 2a + 3a + 4a + \ldots + na = a \frac{n(n+1)}{2} = O(n^2)$
- So logarithmic merging is an order of magnitude more efficient.
Often a combination

- Frequent incremental changes
- Rotation of large parts of the index that can then be swapped in
- Occasional complete rebuild (becomes harder with increasing size – not clear if Google can do a complete rebuild)
Building positional indexes

- Basically the same problem except that the intermediate data structures are large.